

Poker hand consists of 5 cards selected from a deck of 52 cards.

- How many different poker hands are there?
 $C(52,5) = 2598960$ hands $(\{1,2,3,4,5\} = \{5,3,4,2,1\})$
- How many different poker hands consist entirely of aces and kings?
Number of aces + kings = 8; $C(8,5) = 56$ hands.
- How many different poker hands consist entirely of clubs? # of clubs = 13, $C(13,5) = 1287$ hands.
- How many consist of 3 aces and 2 kings? $C(4,3).C(4,2) = 4.6 = 24$
- How many different poker hands consist entirely of red cards?
red cards = 26; $C(26,5) = 65780$ hands.
- How many combinations have cards from exactly 2 suits?
a) Consider one from the 1st suit, then there are $C(4,1) = 4$, and left 4 for the other suit then there are $C(3,1) = 3$. Therefore there are $4.C(13,1) . 3C(13,4) = 111540$ ways.
b) Consider 2 from the 1st suit, then there are $C(4,1) = 4$, and left 3 for the other suit then there are $C(3,1) = 3$. Therefore there are $4.C(13,2) . 3C(13,3) = 267696$ ways
c) Total = $111540 + 267696 = 379236$ ways
- How many ways all the cards from the same suit?
Select a suit, there are $C(4,1) = 4$ ways to do this. For each selection of a suit there are $C(13,5) = 1287$.
Final = $4 . C(13,5) = 5148$ ways.
- How many ways 3 from one suit and 2 from another?
Select a suit, there are $C(4,1) = 4$ ways to do this. The other suit is $C(3,1) = 3$ (since 3 suits left to choose from). First 3 from 1 suit there are $4.C(13,3) = 286$ ways, and 2 from another $3.C(13,2) = 78$.
Total = $4.C(13,3) . 3C(13,2) = 22308$ ways.
- How many ways 2 aces, 2 cards of another denomination, and 1 card of a 3rd denomination.
 - For 2 aces = $C(4,2) = 6$
 - 2 cards of another denomination are $C(4,2) = 6$ ways, there are 12 ways for the 2nd denomination.
Therefore, there are $12.(6) = 72$ ways
 - 3rd denomination there are 11 ways, 1 card $\Rightarrow 11.C(4,1) = 44$
The outcomes: $6.(72).(44) = 19008$ hands.
- How many hands are in 2 cards of 1 denomination, 2 cards of another different denomination, and 1 card of a 3rd denomination.
Select 2 cards of 1 denomination = $C(13,2) = 78$ ways.
Select 2 of one denomination, there are $C(4,2) = 6$
Then select 2 of the other = $C(4,2) = 6$
Select the 3rd denomination, there are $11.C(4,1) = 44$
of poker hands = $78.6.6.44 = 123552$ hands.